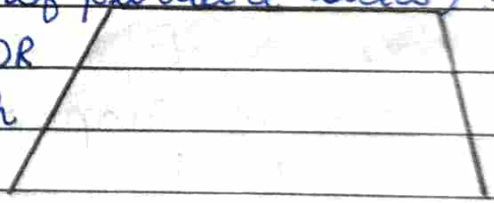


## Chapter-14 Mensuration

1. Area of square = Side  $\times$  Side
2. Area of rectangle =  $l \times b$
3. Area of Triangle =  $\frac{1}{2} \times b \times h$
4. Area of  $\parallel$ gm = Base  $\times$  Height
5. Area of Rhombus =  $\frac{1}{2} \times d_1 \times d_2$
6. Area of circle =  $\pi r^2$
7. Area of Trapezium =  $\frac{1}{2} \times (\text{Sum of parallel sides}) \times h$

$$\frac{1}{2} (a+b) h$$



WS-1

Q1: Here  $a = 57 \text{ cm}$ ,  $b = 33 \text{ cm}$ ,  $h = 13 \text{ cm}$

$$\begin{aligned}
 \text{Area of Trapezium} &= \frac{1}{2} (a+b) h \\
 &= \frac{1}{2} (57+33) 13 \\
 &= \frac{1}{2} \times 90 \times 13 \\
 &= 585 \text{ cm}^2
 \end{aligned}$$

Q2: Here  $a = 64 \text{ cm}$ ,  $h = 17 \text{ cm}$

Let length of other sides be  $b \text{ cm}$

$$\text{Area of Trapezium} = 850 \text{ cm}$$

$$= \frac{1}{2} (a+b)h = 850$$

$$= \frac{1}{2} (64+b) \times 17 = 850$$

$$\Rightarrow 64+b = \frac{850 \times 2}{17}$$

$$\Rightarrow 64+b = 100$$

$$\Rightarrow b = 100 - 64$$

$$\Rightarrow b = 36$$

Q3: Here sum of parallel sides =  $122 \text{ cm}$

$$\text{Area of Trapezium} = 1586 \text{ cm}^2$$

height ( $h$ ) = ?

$$\frac{1}{2} \times (\text{sum of parallel lines}) \times h$$

$$= \frac{1}{2} \times 122 \times h = 1586$$

$$\Rightarrow h = \frac{1586 \times 2}{122}$$

$$\Rightarrow h = 13 \times 2$$

$$= h = 26 \text{ cm}$$

Height =  $26 \text{ cm}$

Q4: Here  $a = 8\text{ m}$   
 $b = 60\text{ dm}$  |  $1\text{ m} = 10\text{ dm}$

$$b = \frac{60}{10}\text{ m} = b = 6\text{ m}$$

Let altitude be  $h\text{ m}$

Area of trapezium =  $28\text{ m}^2$

$$\frac{1}{2}(a+b)h = 28$$

2

$$\frac{1}{2} \times (8+6) \times h = 28$$

2

$$\frac{1}{2} \times 14 \times h = 28$$

2

$$h = \frac{28 \times 2}{14}$$

$$h = 4\text{ m}$$

Q5: Here  $a = 55.6\text{ cm}$ ,  $b = 34.4\text{ cm}$   
 Area of Trapezium =  $1080\text{ cm}^2$   
 Let altitude be  $h\text{ cm}$

$$\frac{1}{2}(a+b)h$$

2

$$= \frac{1}{2} \times (55.6 + 34.4) \times h = 1080$$

$$= \frac{1}{2} \times 90 \times h = 1080$$

2

$$h = \frac{1080 \times 2}{90}$$

$$h = 24$$

Q6: Height of Trapezium ( $h$ ) =            m  
 Area of Trapezium =  $12 \text{ m}^2$

$$\frac{1}{2} (\text{Sum of parallel sides}) \times h = 12 \text{ m}^2$$

$$\frac{1}{2} \times (\text{Sum of parallel sides}) \times 3 = 12 \text{ m}^2$$

$$\text{Sum of parallel sides} = \frac{12 \times 2}{3} = 8 \text{ m}$$

Q7: Let 2 parallel sides be  $x \text{ m}$  and  $(x-4) \text{ m}$   
 height ( $h$ ) =  $8 \text{ m}$   
 Area of Trapezium =  $248 \text{ m}^2$

$$\frac{1}{2} (\text{Sum of parallel sides}) \times h$$

$$\frac{1}{2} (x + x - 4) \times 8 = 248 \text{ m}^2$$

$$2x - 4 = \frac{248}{4} \times 2$$

$$2x = 62 + 4$$

$$2x = 66$$

$$x = \frac{66}{2} = 33$$

Q8: Let parallel sides be  $x \text{ dm}$  and  $(x+8) \text{ dm}$   
 Altitude ( $h$ ) =  $10 \text{ dm}$

$$\text{Area of Trapezium} = 1.6 \text{ m}^2$$

$$= 1.6 \times 100 \text{ dm}^2$$

$$\frac{1}{2} (\text{Sum of parallel sides}) \times h = 160 \text{ dm}^2$$

$$\frac{1}{2} \times (x + x + 8) \times 5 = 160$$

$$2x + 8 = \frac{160}{5} \times 2$$

$$2x = 32 - 8$$

$$x = \frac{24}{2}$$

$$x = 12$$

So sides are 12 dm &  $12 + 8$  dm = 20 dm  
 Area = 160 dm<sup>2</sup>

Q9. Area of cross section of canal = 138 m<sup>2</sup>

$$a = 15 \text{ m}$$

$$b = 8 \text{ m}$$

$$\frac{1}{2} \times (a + b) \times h$$

$$= \frac{1}{2} \times (15 + 8) \times h = 138 \text{ m}$$

$$= \frac{1}{2} \times 23 \times h = 138$$

$$h = \frac{138 \times 2}{23}$$

$$h = 12 \text{ m}$$

Q11: Let parallel sides be  $4x$  m and  $7x$  m

$$\text{Height} = 14 \text{ m}, \text{ Area} = 385 \text{ m}^2$$

$$\text{Area} = \frac{1}{2} \times (4x + 7x) \times 14 = 385$$

$$\frac{1}{2} \times 11x \times 14 = 385 = 11x = \frac{385}{1}$$

$$x = \frac{35}{1} \text{ So sides are } 20 \text{ m \& } 35 \text{ m}$$

v. simple

Q10: Let ABCD is a given trapezium  
in which  $AB = 58\text{ m}$

$$CD = 42\text{ m}$$

$$AD = BC = 17\text{ m}$$

Through C draw  $CF \parallel AD$

Also  $CE \perp AB$

Now  $AF \parallel CD$  | given

$AD \parallel CF$  | By construction

So AFCD is a ||gm

$$AF = CD = 42\text{ cm}$$

$$AD = CF = 17\text{ cm}$$

$$FB = AB - AF = 58 - 42$$

$$= 16\text{ cm}$$

In  $\triangle FBC$ ,  $FB = BC = 17\text{ cm}$

So it is isosceles triangle

Also  $CF \perp FB$  so E is the midpoint of FB

$$FE = \frac{1}{2} \times 16 = 8\text{ cm}$$

In right angled  $\triangle CFE$  by pythagoras Theorem

$$FE^2 + CE^2 = CF^2$$

$$8^2 + h^2 = 17^2$$

$$64 + h^2 = 289$$

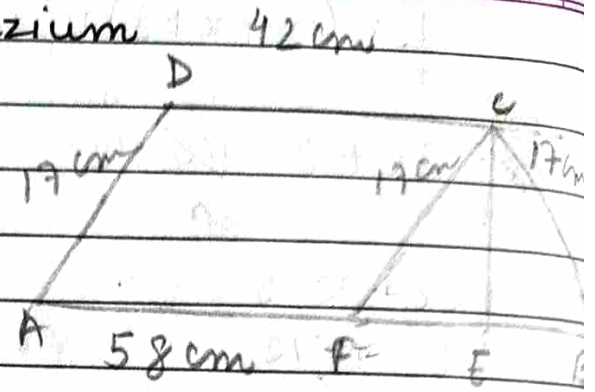
$$h^2 = 289 - 64$$

$$h^2 = 225$$

$$h = 15\text{ cm}$$

$$\text{Area of trapezium} = \frac{1}{2} (\text{Sum of parallel sides}) h$$

$$= \frac{1}{2} (58 + 42) \times 15$$



$$\frac{1}{2} \times 100 \times 15$$

$$= 750 \text{ cm}^2$$

Q12. Perimeter of Trapezium = 104 m

Altitude (h) = 16 m

Sum of non parallel sides = (18 + 22) m  
= 40 m

Sum of parallel sides = 104 - 40  
(a + b) = 64 m

Area of Trapezium =  $\frac{1}{2} (a+b) h$

$$= \frac{1}{2} (64) \times 16$$

$$= 512 \text{ m}^2$$

WS-2

Q1: Find the area

(i) Area of quadrilateral PQRS = Area  $\Delta$  PQS + Area  $\Delta$  SRQ

$$= \frac{1}{2} \times 50 \times 4 + \frac{1}{2} \times 7 \times 3$$

$$= 14 + \frac{21}{2}$$

$$= 14 + 10.5$$

$$= 24.5 \text{ cm}^2$$

(iii) Area of polygon  
 Area of trap. ACDE + Area of  $\triangle ABC$   

$$= \frac{1}{2} (12+8) \times 2 + \frac{1}{2} \times 12 \times 4 \times 2$$

$$= 20 + 24$$

$$= 44 \text{ cm}^2$$

Q2 (ii) Area of polygon = Area of  $\triangle FED$  + Area  $\triangle FCD$  +  
 Area  $\triangle FBC$  + Area  $\triangle FBA$   

$$= \left( \frac{1}{2} \times 5 \times 2 \right) + \left( \frac{1}{2} \times 7 \times 4 \right) + \left( \frac{1}{2} \times 7 \times 4 \right) + \left( \frac{1}{2} \times 6.5 \times 2 \right)$$

$$= 5 + 14 + 14 + 6.5$$

$$= 39.5 \text{ cm}^2$$

Q3: Since it is a regular octagon so all sides are 5m  
 Area of octagon = Area of Trapezium ABCH + Area  
 of trap. GFED + Area of rectangle CDGH  

$$= \frac{1}{2} (11+5) \times 4 + \frac{1}{2} (11+5) \times 4 + 11 \times 5$$

$$= 16 \times 2 + 16 \times 2 + 55$$

$$= 32 + 32 + 55$$

$$= 119 \text{ m}^2$$

TSA of cube - 6 side<sup>2</sup>

L.S.A. of cube - 4 side<sup>2</sup>

TSA of cuboid - 2(lb + bh + hl)

L.S.A of cuboid - 2h(l+b)



Q4: Neha fig

$$\begin{aligned} \text{Req. area} &= 2 \times \text{Area of Trapezium} \\ &= 2 \times \frac{1}{2} (25 + 15) 6 \end{aligned}$$

$$= 43 \times 6$$

$$= 258 \text{ cm}^2$$

Nidhi's fig

$$\begin{aligned} \text{Req. area} &= \text{Area of triangle} + \text{Area of rectangle} \\ &= \frac{1}{2} \times 6 \times 13 + 12 \times 15 \end{aligned}$$

$$= 78 + 180$$

$$= 258 \text{ m}^2$$

WS-3

Q1: T.S.A. of cube =  $600 \text{ cm}^2$

$$6 \text{ side}^2 = 600$$

$$\text{side}^2 = \frac{600}{6} = 100$$

$$\text{side} = 10$$

$$\text{So side} = 10 \text{ cm}$$

Q2: Length of room =  $(l) = 5 \text{ m}$

Breadth of room =  $4 \text{ m}$

Height of room =  $3 \text{ m}$

$$\begin{aligned} \text{Area of 4 walls and ceiling} &= 2h(l+b) + lb \\ &= 2 \times 3(5+4) + 5 \times 4 \\ &= 6 \times 9 + 20 \end{aligned}$$

$$74 \text{ m}^2$$

$$\text{cost of white washing } 1 \text{ m}^2 = ₹ 50$$

$$\begin{aligned} \text{Cost of white washing } 74 \text{ m}^2 &= ₹ 50 \times 74 \\ &= ₹ 3700 \end{aligned}$$

Q3: Length of box =  $0.5 \text{ m} = 50 \text{ cm}$

Breadth of box =  $25 \text{ cm}$

Height of box =  $15 \text{ cm}$

$$\text{T.S.A of box} = 2(lb + bh + hl)$$

$$= 2(50 \times 25 + 25 \times 15 + 15 \times 50)$$

$$= 2(1250 + 375 + 750)$$

$$= 4750 \text{ cm}^2$$

Q4: For cuboidal box:-

$$l = 50 \text{ cm}$$

$$b = 40 \text{ cm}$$

$$h = 30 \text{ cm}$$

$$\text{T.S.A of cuboid} = 2(lb + bh + hl)$$

$$= 2(50 \times 40 + 40 \times 30 + 30 \times 50)$$

$$= 2(2000 + 1200 + 1500)$$

$$= 2 \times 4700$$

$$= 9400 \text{ cm}^2$$

For cubical box

$$\text{Side} = 40 \text{ cm}$$

$$\text{T.S.A of cube } 6 \text{ side}^2$$

$$6 \text{ side}^2 = 40$$

$$= 6 \times 40^2$$

$$= 6 \times 1600$$

$$= 9600 \text{ cm}^2$$

Q5: For cuboidal box

$$L = 26 \text{ cm}$$

$$B = 26 \text{ cm}$$

$$h = 45 \text{ cm}$$

$$\begin{aligned} \text{Area of req. tin for 1 box} &= 2(lb + bh + hl) \\ &= 2(26 \times 26 + 26 \times 45 + 45 \times 26) \\ &= 2(676 + 1170 + 1170) \\ &= 2 \times 3016 \\ &= 6032 \text{ cm}^2 \end{aligned}$$

$$\begin{aligned} \text{Area of tin req. for 20 boxes} &= 20 \times 6032 \\ &= 120640 \text{ cm} \end{aligned}$$

Q6: L of swimming pool = 20 m

B of swimming pool = 15 m

D of swimming pool = 4 m

$$\begin{aligned} \text{Area to be cemented} &= 2h(l+b) + lb \\ &= 2 \times 4(20+15) + 20 \times 15 \\ &= 8 \times 35 + 300 \\ &= 280 + 300 \\ &= 580 \text{ m}^2 \end{aligned}$$

$$\text{Cost of cementing } 1 \text{ m}^2 = ₹ 35$$

$$\begin{aligned} \text{Cost of cementing } 580 \text{ m}^2 &= 580 \times 35 \\ &= ₹ 20300 \end{aligned}$$

Q7: Length of cubical box = 30 cm

Area to

Since it is painted from inside & outside also

$$\begin{aligned}
 \text{req area} &= 2 \times \text{T.S.A of cube} \\
 &= 2 \times 6 \text{side}^2 \\
 &= 2 \times 6 \times 30 \times 30 \\
 &= 10800 \text{ cm}^2 \\
 &= \frac{10800}{100 \times 100} = 1.08 \text{ m}^2
 \end{aligned}$$

$$\begin{aligned}
 \text{cost of painting } 1 \text{ m}^2 &= ₹ 5.50 \text{ m}^2 \\
 \text{Cost of painting } 1.08 \text{ m}^2 &= 1.08 \times 5.50 \\
 &= ₹ 5.94
 \end{aligned}$$

Q8: when two cubes of sides 4cm are fixed together we get a cuboid of 8cm  
 Length = 8cm, Breadth = 4cm, Height = 4cm

$$\begin{aligned}
 \text{T.S.A of cuboid} &= 2(lb + bh + hl) \\
 &= 2(8 \times 4 + 4 \times 4 + 4 \times 8) \\
 &= 2(32 + 16 + 32) \\
 &= 2(64 + 16) \\
 &= 2 \times 80 \\
 &= 160 \text{ cm}^2
 \end{aligned}$$

$$\begin{aligned}
 \text{C.S.A of cylinder} &= 2\pi rh \\
 \text{T.S.A of cylinder} &= 2\pi rh + 2\pi r^2 \\
 &= 2\pi r(h+r)
 \end{aligned}$$

WS-4

Q1: For right cylinder  
 $h = 15$        $R = 7 \text{ cm}$

$$\text{CSA of cylinder} = 2\pi rh$$

$$= \frac{2 \times 22 \times 7 \times 15}{7}$$

$$= 660 \text{ cm}^2$$

$$\begin{aligned} \text{T.S.A. of cylinder} &= 2\pi r(h+r) \\ &= \frac{2 \times 22 \times 7 \times (7+5)}{7} \end{aligned}$$

$$\begin{aligned} &= 2 \times 22 \times 12 \\ &= 968 \text{ cm}^2 \end{aligned}$$

Q2: For Right circular Cylinder :-

Diameter = 4.2 dm

$$r = \frac{4.2}{2} = 2.1 \text{ dm}$$

$$= 2.1 \times 10 \text{ cm}$$

$$= 21 \text{ cm}$$

$$h = 1 \text{ dm} = 10 \text{ cm}$$

$$\begin{aligned} \text{C.S.A of Cylinder} &= 2\pi rh \\ &= \frac{2 \times 22 \times 2.1 \times 10}{7} \end{aligned}$$

$$= 1320 \text{ cm}^2$$

Q3: R = 10.5 cm, h = ?

C.S.A of cylinder = 1320 cm<sup>2</sup>

$$2\pi rh = \frac{2 \times 22 \times 10.5 \times h}{7} = 1320$$

$$h = \frac{1320 \times 7 \times 10}{2 \times 22 \times 105}$$

$$h = 20 \text{ cm}$$

Q4: Height of cylinder ( $h$ ) = 65 cm  
Circumference of cylinder = 176 cm  
 $2\pi r = 176$

C.S.A of cylinder =  $2\pi rh$   
=  $176 \times 65$   
=  $1440 \text{ cm}^2$

~~Q5: For first cylinder~~

Q5: Let radii of 2 cylinders be  $2x$  and  $3x$  and Heights be  $5y$  and  $3y$

Ratio =  $\frac{\text{C.S.A of 1st cylinder}}{\text{C.S.A of 2nd cylinder}}$

=  $\frac{2\pi \times 2x \times 5y}{2\pi \times 3x \times 3y} = \frac{10}{9}$

= 10:9

Q6: Diameter = 20 cm

$r = 10 \text{ cm}$

$h = 70 \text{ cm}$

C.S.A of cylinder =  $2\pi rh$   
=  $2 \times \frac{22}{7} \times 10 \times 70$   
=  $4400 \text{ cm}^2$

Cost of painting  $1 \text{ cm}^2 = ₹4$

Cost of painting  $4400 \text{ cm}^2 = 4400 \times 4$   
= ₹17600

Q7:  $r = 10 \text{ cm}$   
 $h = 14 \text{ cm}$   
 $\pi = 3.14 \text{ cm}$

Since cylindrical vessel is opened at top

$$\text{T.S.A of vessel} = 2\pi rh + \pi r^2$$

$$= \pi r (2h + r)$$

=

$$= 3.14 \times 10 (28 + 10)$$

$$= 31.4 \times 38$$

$$= 1193.2 \text{ cm}^2$$

Q8: Length of roller = (h) = 40 cm = 0.4 m

$$d = 21 \text{ cm}$$

$$r = \frac{21}{2} \text{ cm}$$

$$\text{C.S.A of cylinder} = 2\pi rh$$

$$= 2 \times \frac{21}{2} \times 21 \times 40$$

$$= 66 \times 40 = 2640 \text{ cm}^2$$

$$\text{Area covered in 1 revolution} = 2640 \text{ cm}^2$$

$$\text{Area covered in 300 revolutions} = 2640 \times 300$$

$$= 792000 \text{ cm}^2$$

$$= \frac{792000}{10,000} \text{ cm}^2$$

$$= 79.2 \text{ m}^2$$

$$= 79.3 \text{ m}^2$$

Q9: For closed metallic cylinder diameter = 56 cm  
 $r = 28 \text{ cm} = 0.28 \text{ m}$   
 $h = 2.25 \text{ m}$

Area of metal sheet used = T.S.A. of cylinder  
 $= 2\pi r(r+h)$

$$= \frac{2 \times 22}{7} \times 0.28 (0.28 + 2.25)$$

$$= \frac{2 \times 22 \times 28}{100} (2.53)$$

$$= \frac{176}{100} \times 2.53 \text{ m}^2$$

$$= \frac{445.28}{100} = 4.4528$$

Cost of  $1 \text{ m}^2$  metal = ₹ 80

$$\text{Cost of } 4.4528 \text{ m}^2 = 4.4528 \times 80$$

$$= ₹ 356.22$$

Q10

Length of rectangular paper = 22 cm

Breadth of rectangular paper = 10 cm

Since it is rolled along its length to get cylinder  
 So circumference of cylinder = length of paper

$$2\pi r = 22 \text{ cm}$$

Height of cylinder ( $h$ ) = Breadth of paper  
 $h = 10 \text{ cm}$

$$\text{S.A. of cylinder} = 2\pi r h$$

$$= 22 \times 10$$

$$= 220 \text{ cm}^2$$



Outer diameter = 21m

$R = 10.5m$

Inner Diameter = 14m

$r = 7 + 0.5m$

$h = 21$

Inner C.S.A. + Outer C.S.A.

$2\pi rh + 2\pi R h$

$= 2\pi (r + R) h$

$= 2 \times \frac{22}{7} \times 17.5 \times (7 + 10.5)$

$= 132 \times 17.5$

Cost

$1m^2 = ₹ 25$

$₹ 25 \times 132 \times 17.5$

$= ₹ 71750$

WS - 5

Q1: When 2 cubes of same side 6cm joined together we get a cuboid of

$L = 6 + 6 = 12cm$

$B = 6cm$

$H = 6cm$

V. of cuboid =  $l \times b \times h$

$= 12 \times 6 \times 6$

$= 12 \times 36$

$= 432 cm^3$

2. Base area of cuboid ( $l \times b$ ) =  $25 \text{ cm}^2$

Volume of cuboid =  $275 \text{ cm}^3$

$$l \times b \times h = 275$$

$$25 \times h = 275$$

$$h = \frac{275}{25}$$

$$h = 11$$

$$h = 11 \text{ cm}$$

Q3: Dimensions of cuboid

$$l = 60 \text{ cm}$$

$$b = 54 \text{ cm}$$

$$h = 30 \text{ cm}$$

Side of cube =  $6 \text{ cm}$

No. of cube which can be placed in cuboid

$$= \frac{\text{V. of cuboid}}{\text{V. of cube}}$$

$$= \frac{l \times b \times h}{\text{side}^3}$$

$$= \frac{60 \times 54 \times 30}{6 \times 6 \times 6}$$

$$= \frac{10^1 \times 9^1 \times 5^1}{6 \times 6 \times 6}$$

$$= 450 \text{ cubes}$$

Q5: Dimension of cuboid

$$l = 4 \text{ cm}$$

$$b = 2.5 \text{ cm}$$

$$h = 1.5 \text{ cm}$$

Volume of 1 match box =  $l \times b \times h$

$$\begin{aligned} \text{Volume of 12 math box} &= 12 lbh \\ &= 12 \times 4 \times 2.5 \times 1.5 \\ &= 180 \text{ cm} \end{aligned}$$

Q4: Let original edge of cube be  $x$  units when edge is doubled, So now:-

$$\text{Edge} = 2x \text{ units}$$

$$(i) \text{ Original S.A.} = 6x^2$$

$$\text{New S.A.} = 6(2x)^2$$

$$= 6 \times 4x$$

$$= 4 \times 6x^2$$

$$= 4x \text{ is the original S.A.}$$

So S.A. becomes 4 times

$$(ii) \text{ Original volume } x^3$$

$$\text{New volume} = (2x)^3$$

$$= 8x^3$$

$$= 8x \text{ is the original volume}$$

So volume becomes 8 times

$$Q6: \text{ volume of cube} = 1000 \text{ cm}^3$$

$$\text{Side}^3 = 1000$$

$$\text{Side}^3 = \sqrt[3]{1000}$$

$$\text{Side} = 10 \text{ cm}$$

$$\text{T.S.A of cube} = 6 \text{ side}^2$$

$$6 \times 10^2$$

$$6 \times 100$$

$$= 600 \text{ cm}^2$$

Q7: Dimensions of wooden block plank

$$l = 6\text{m} = 600\text{cm}, b = 15\text{cm} \quad h = 40\text{cm}$$

Dimensions of the plank are, length =

$$L = 2\text{m} = 200\text{cm} \quad B = 2.5\text{cm} \quad h = 4\text{cm}$$

Since planks are to cut off from wooden block

$$\text{No. of planks} = \frac{\text{No. of wooden block}}{\text{V. of planks}}$$

$$= \frac{600 \times 15 \times 40}{200 \times 2.5 \times 4}$$

$$= \frac{3 \times 10^3 \times 10^2}{25}$$

$$= 180 \text{ planks}$$

Q8: Edges of 3 small cubes are 6 cm, 8 cm, 10 cm

Since 3 cubes melted to form a big cube

So V. of big cube = Sum of volume of 3 small cubes

$$= 6^3 + 8^3 + 10^3$$

$$= 1728$$

Q9: S. A. of cube = 150 m<sup>2</sup>

$$6 \text{ side}^2 = 150$$

$$\text{side}^2 = \frac{150}{6}$$

$$\text{side} = 5\text{m}$$

$$\begin{aligned} \text{volume of cube} &= \text{side}^3 \\ &= 5^3 \\ &= 125 \text{ m}^3 \end{aligned}$$

Q10: Area of one face of cube =  $81 \text{ m}^2$   
 $\text{Side}^2 = 81 \text{ m}^2$   
 $\text{Side} = 9 \text{ m}$

$$\begin{aligned} \text{volume of cube} &= \text{side}^3 \\ &= 9^3 \\ &= 729 \text{ m}^3 \end{aligned}$$

WS-6

Q1:  $r = 7 \text{ cm}$

$h = 15 \text{ cm}$

$\pi r^2 h = 154 \text{ cm}$

Volume of cylinder =  $\pi r^2 h$

$154 \times 15$

$= 231 \text{ cm}^3$

Q2: height of cylinder ( $h$ ) =  $25 \text{ cm} = 0.25 \text{ m}$

Circumference of base =  $1.32 \text{ m}$

$2\pi r = 1.32 \text{ m}$

$r = \frac{1.32}{2\pi}$

$2\pi$

$\frac{3}{7}$

$= 132 \times 7$

$100 \times r \times 2r$

$= 0.21 \text{ or } \frac{21}{100}$

$$V. \text{ of cylinder} = \pi r^2 h$$

$$\frac{22 \times 21}{7} \times \frac{21}{100} \times \frac{25}{100}$$

$$= \frac{34650}{100000}$$

$$= 0.03465 \text{ m}^3$$

Q2:  $h = 16 \text{ m}$   
 $d = 7 \text{ m}$   
 $r = \frac{7}{2} \text{ m}$

Req. amount of earth = V. of cylinder

$$= \pi r^2 h$$

$$\frac{22}{7} \times 7 \times 7 \times 16$$

$$= 616 \text{ m}^3$$

Q3: Diameter = 28 m

$$r = 14 \text{ m}$$

$$h = 7 \text{ m}$$

Amount of water it can hold = V. of cylinder

$$= \pi r^2 h$$

$$= \frac{22}{7} \times 14 \times 14 \times 7$$

$$= 4312 \text{ kl}$$

$$| 1 \text{ kl} = 1 \text{ m}^3$$

Q4: For cylindrical oil can

$$r = 4 \text{ m}$$

Amount of oil it can hold

$$\pi r^2 h = 1408 \text{ kl}$$

$$\frac{22 \times 14 \times 14 \times h}{7} = 1408 \text{ m}^3$$

$$h = \frac{1408 \times 7}{22 \times 14 \times 14}$$

$$h = 28 \text{ m}$$

Q 5: Let radius and height of cylinder are  $5x \text{ cm}$  &  $7x \text{ cm}$

$$\text{Volume} = 550 \text{ cm}^3$$

$$\pi r^2 h = 550$$

$$\frac{22 \times 5x \times 5x \times 7x}{7} = 550$$

$$x^3 = \frac{550}{22 \times 5 \times 5} = 1$$

$$x = 1$$

$$\text{So radius } 5x = 5 \text{ cm}$$

$$\text{Height } 7x = 7 \text{ cm}$$

Q 6: For hollow metallic cylinder

$$h = 35 \text{ cm}$$

$$\text{Inner radius } (r) = 12 \text{ cm}$$

$$\text{Thickness} = 2 \text{ cm}$$

$$\text{Outer radius } (R) = 12 + 2 = 14 \text{ cm}$$

Since it is opened from both ends

Volume of metal required

$$\text{Outer V.} - \text{Inner V.}$$

$$\pi R^2 h - \pi r^2 h$$

$$= \pi h (R^2 - r^2)$$

$$= \frac{22}{7} \times 35 (14^2 - 12^2)$$

$$110 (196 - 144)$$

$$110 \times 52$$

$$= 5720 \text{ cm}^3$$

Q7: length of rectangular sheet = 33 cm

Breadth = 32 cm

Since sheet is rolled along its length to make cylinder  
so circumference of cylinder = 33 cm

$$2\pi r = 33$$

$$r = \frac{33}{2\pi} = \frac{33 \times 7}{22 \times 2}$$

$$r = \frac{21}{4}$$

height of cylinder (h) = 32 cm

Capacity of cylinder =  $\pi r^2 h$

$$= \frac{22}{7} \times \frac{21}{4} \times \frac{21}{4} \times 32$$

$$= 2772 \text{ cm}^3$$

Q8: Height of cylinder = 6 cm

Volume of cylinder =  $150\pi$

$$\pi r^2 h = 150\pi$$

$$r^2 \times 6 = 150$$

$$r^2 = \frac{150}{6} = 25$$

$$= r^2 = 5$$

T.S.A =  $2\pi r (r + h)$

$$= \frac{2 \times 22}{7} \times 5 (5 + 6) = \frac{2420}{7} = 345 \frac{5}{7}$$



Q8: For 2 cylinders

$$h_1 = 49 \text{ cm}$$

$$h_2 = 35 \text{ cm}$$

$$d_1 = 16 \text{ cm}$$

$$d_2 = 14 \text{ cm}$$

$$r_1 = 8 \text{ cm}$$

$$r_2 = 7 \text{ cm}$$

Since both cylinders are melted to form a single cylinder of height ( $h$ ) = 56 cm

→ Sum of volume of 2 cylinders = V. of big cylinder

$$= \pi r_1^2 h_1 + \pi r_2^2 h_2 = \pi R^2 H$$

$$\pi (r_1^2 h_1 + r_2^2 h_2) = \pi R^2 H$$

$$= 8^2 \times 49 + 7^2 \times 35 = R^2 \times 56$$

$$= 49(64 + 35) = R^2 \times 56$$

$$= 49 \times 99 = R^2 \times 56$$

$$= \frac{49 \times 99}{56} = R^2$$

$$568$$

$$R^2 = \frac{693}{8} = 86.625$$

$$R = 9.3$$

$$D = 18.6 \text{ cm}$$

Q9: For metallic cylindrical pipe

$$h = 14 \text{ cm}$$

External Radius ( $R$ ) = 9 cm

Let internal Radius be  $r$  cm

Volume of metal = 748 cm<sup>3</sup>

$$\pi R^2 h - \pi r^2 h = 748$$

$$\pi h (R^2 - r^2) = 748$$

$$\frac{22 \times 14 (9^2 - r^2)}{7} = 748$$

$$44 (81 - r^2) = 748$$

$$81 - r^2 = \frac{748}{44} = 17$$

$$= r^2 = 81 - 17$$

$$= r^2 = 64$$

$$= r = 8 \text{ cm}$$

$$\text{So thickness } R - r = 9 - 8$$

$$= 1$$

Q11: Volume of cylindrical pillar =  $924 \text{ m}^3$

$$\pi r^2 h = 924 \quad \text{--- 1}$$

C.S.A. of cylindrical pillar =  $264 \text{ m}^2$

$$2\pi r h = 264 \quad \text{--- 2}$$

Dividing 1 by 2

$$\frac{\pi r^2 h}{2\pi r h} = \frac{924}{264}$$

$$\frac{r}{2} = \frac{924}{264}$$

$$\frac{r}{2} = 7$$

$$r = 7 \times 2$$

$$2\pi (7) h = 264$$

$$2 \times 22 \times 7 \times h = 264$$

$$h = \frac{264 \times 7}{2 \times 22 \times 7}$$

$$h = 2$$

So height of pillar is 6 cm

$$r = 7 \text{ cm}$$

$$\text{So } d = 2 \times 7 = 14 \text{ cm}$$

WS-8

Q1- Done in book

Q2- Done in book

Q3: No, because in square prism all the faces may not be a square

Q4: (i)  $F = 6$

$$V = 8$$

$$E = 12$$

$$F + V - E = 2$$

$$6 + 8 - 12 = 2$$

$$2 = 2$$

$$\text{LHS} = \text{RHS}$$

Hence verified

(ii)  $F = 9$

$$E = 16$$

$$V = 9$$

$$F + V - E = 2$$

$$9 + 9 - 16 = 2$$

$$2 = 2$$

$$\text{LHS} = \text{RHS}$$

Hence verified

(iii)  $F = 5$

$$E = 8$$

$$V = 5$$

$$F + V - E = 2$$

$$5 + 5 - 8 = 2$$

$$10 - 8 = 2$$

$$2 = 2$$

$$\text{LHS} = \text{RHS}$$

Hence verified

(iv)  $F = 5$

$$E = 8$$

$$V = 5$$

$$F + V - E = 2$$

$$5 + 5 - 8 = 2$$

$$10 - 8 = 2$$

$$2 = 2$$

$$\text{LHS} = \text{RHS}$$

Hence verified

Q5: (i)  $F=8, E=12, V=?$

$$F+V-E=2$$

$$8+V-12=2$$

$$-4+V=2$$

$$V=2+4$$

$$V=6$$

(iii)  $F=10, V=12, E=?$

$$F+V-E=2$$

$$10+12-E=2$$

$$22-E=2$$

$$-E=2-22$$

$$-E=-20$$

$$=E=20$$

(ii)  $F=?, E=9, V=6$

$$F+V-E=2$$

$$F+6-9=2$$

$$F=2+3$$

$$F=5$$

Q6:  $F=10$

$$E=20$$

$$V=15$$

$$F+V-E=2$$

$$10+15-20=2 = 25-20=2$$

$$5=2$$

$\therefore$  So no it is not a polyhedron.

### Value Based Questions

Q1: a) For a room the dimensions are -

$$L = 10\text{ m}$$

$$B = 12\text{ m}$$

$$h = 3.5\text{ m}$$

Area of 4 walls and ceiling =  $2h(l+b) + lb$

$$2 \times 3.5(10+12) + 10 \times 12$$

$$7 \times 22 + 120$$

$$= 274\text{ m}^2$$

For second room the dimensions are -

$$l = 8 \text{ m}$$

$$b = 6 \text{ m}$$

$$h = 3.5 \text{ m}$$

$$\begin{aligned} \text{Area of 4 walls and ceiling} &= 2h(l+b) + lb \\ &= 2 \times 3.5(8+6) + 8 \times 6 \\ &= 7 \times 14 + 48 \\ &= 146 \text{ m}^2 \end{aligned}$$

For third room the dimensions are -

$$l = 7 \text{ m}$$

$$b = 5 \text{ m}$$

$$h = 3.5 \text{ m}$$

$$\begin{aligned} \text{Area of 4 walls and ceiling} &= 2h(l+b) + lb \\ &= 2 \times 3.5(7+5) + 7 \times 5 \\ &= 7 \times 12 + 35 \\ &= 119 \text{ m}^2 \end{aligned}$$

$$\begin{aligned} \text{Total Area of 3 rooms} &= (274 + 146 + 119) \text{ m}^2 \\ &= 539 \text{ m}^2 \end{aligned}$$

$$\text{Cost of painting } 1 \text{ m}^2 = ₹ 30$$

$$\begin{aligned} \text{Cost of painting } 539 \text{ m}^2 &= 539 \times 30 \\ &= ₹ 16170 \end{aligned}$$

Q1: b) Amount of money given to orphanage =  $\frac{1}{5}$  of ₹ 16170

$$= ₹ 3234 \quad \frac{1}{5} \times 16170$$

c) Caring, Helpful, Kind

Q2: a) Area of Trapezium =  $\frac{1}{2}(a+b)h$

$$= \frac{1}{2}(90+60)50 = 150 \times 25$$

$$= 3750$$

b. Girl education is must

c. Encourage people to send girls to school.

## Brain Teasers

Q1: Tick

(A) a) Side of cube = 0.01m  
 $= 0.01 \times 100$   
 $= 1\text{cm}$

$$\text{Volume} = \text{Side}^3$$
$$1 \times 1 \times 1$$
$$= 1\text{cm}^3$$

b. radius = (r)

height = (h)

$$V. \text{ of cylinder} = \pi r^2 h$$

new radius = r

$$\text{new height} = \frac{h}{2}$$

$$\text{new } V. = \frac{\pi r^2 h}{2} = \frac{1}{2} (\pi r^2 h)$$

$$= \frac{1}{2} \text{ times}$$

c. a = 10cm, b = 12cm, h = 4cm

$$\text{Area of trap.} = \frac{1}{2} (a+b)h$$

$$= \frac{1}{2} (10+12) \times 4$$

$$22 \times 2$$
$$= 44\text{cm}^2$$

d) Triangular pyramid  
= 4 Ans

e) Original cube

Side  $\neq x$

$$V = x^3$$

New cube

side =  $2x$

$$V = 8x^3$$

$$\frac{V. \text{ of new cube}}{V. \text{ of original cube}} = \frac{8x^3}{x^3} = 8:1$$

B b.  $V. \text{ of cube} = 729 \text{ m}^3$

$$\text{Side}^3 = 729$$

$$\text{Side} = 9 \text{ m}$$

$$\begin{aligned} \text{S.A. of cube} &= 6 \text{ side}^2 \\ &= 6 \times 9 \times 9 \\ &= 486 \text{ m}^2 \end{aligned}$$

c) For cylinder

$$D = 12 \text{ cm}$$

$$r = 6 \text{ cm}$$

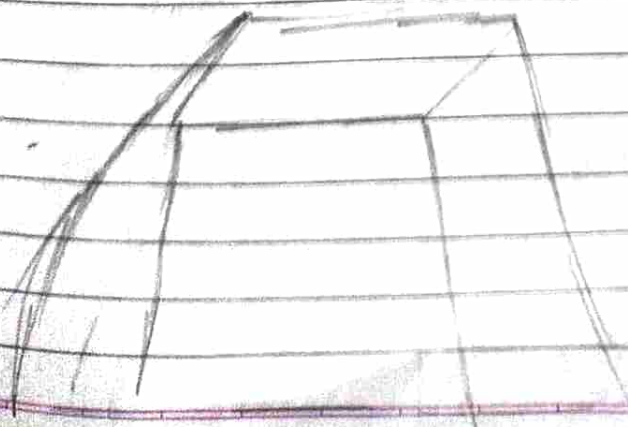
$$V. \text{ of cylinder} = 2376 \text{ cm}^3$$

$$\pi r^2 h = 2376$$

$$\frac{22}{7} \times 6 \times 6 \times h = 2376$$

$$h = \frac{2376 \times 7}{22 \times 6 \times 6} = 21 \text{ cm}$$

d)



e)  $l = 10 \text{ cm}$ ,  $b = 8 \text{ cm}$ ,  $h = 6 \text{ cm}$   
 T.S.A. of cuboid =  $2(lb + bh + hl)$   
 $2(80 + 48 + 60)$   
 $= 376 \text{ cm}^2$

Q2: Area of quadr. = Area of  $\triangle ABC$  + Area of  $\triangle ACD$   
 $= \left(\frac{1}{2} \times 6 \times 3.8\right) + \left(\frac{1}{2} \times 6 \times 7.2\right)$   
 $= 11.4 + 21.6$   
 $= 33 \text{ cm}^2$

Q3: Let 2 // sides of trapezium be  $x \text{ m}$  and  $2x \text{ m}$   
 Distance between // sides  
 $(h) = 100 \text{ m}$

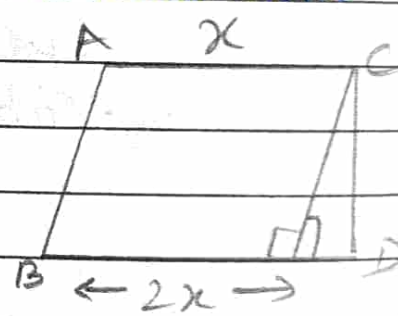
Area of Trapezium =  $10,500 \text{ m}^2$

$\frac{1}{2} (\text{Sum of parallel sides}) h = 10,500$   
 $\frac{1}{2} (x + 2x) 100 = 10,500$

$\Rightarrow 3x = \frac{10500}{50} = 210$

$\Rightarrow x = \frac{210}{3} = 70$

So // sides are  $70 \text{ m}$  &  $2 \times 70 = 140 \text{ m}$



Q4: Let in fig  $ABED$  in given trapezium in which  
 $AB = 36 \text{ cm}$ ,  $CD = 12 \text{ cm}$   
 $AD = BC = 15 \text{ cm}$   
 through C draw  $CE \parallel AD$   
 Draw  $CF \perp AB$

$EB = 36 - 12 = 24 \text{ cm}$

In  $\triangle CEB$   $CE = BC = 15 \text{ cm}$



So it is isosceles triangle

CE ⊥ FB, so F is midpoint EF = FB = 12 cm

In Right angled triangle CFE by Pythagoras th.

$$CF^2 + EF^2 = CE^2$$

$$= h^2 + 12^2 = 15^2$$

$$= h^2 + 144 = 225$$

$$= h^2 = 225 - 144$$

$$= h^2 = 81 \quad , \quad h = 9 \text{ cm}$$

So area of trapezium ABCD =  $\frac{1}{2} (AB + CD)h$

$$= \frac{1}{2} (36 + 12) \times 9$$

$$= \frac{1}{2} \times 48 \times 9$$

$$= 216 \text{ m}^2$$

So req. area is  $216 \text{ m}^2$

Q5: For cuboidal box

$$l = 2 \text{ m } 10 \text{ cm} = 210 \text{ cm}$$

$$b = 1 \text{ m } = 100 \text{ cm}$$

$$h = 80 \text{ cm}$$

Area of canvas required to cover the box = T.S.A of cuboid

$$= 2(lb + bh + hl)$$

$$= 2(210 \times 100 + 100 \times 80 + 80 \times 210)$$

$$= 2(21000 + 8000 + 16800)$$

$$= 2(45800) \text{ cm}^2$$

$$= \frac{91600 \text{ cm}^2}{100 \times 100}$$

$$= 9.16 \text{ m}^2$$

$$= 9.16 \text{ m}^2$$

Q6: Inner Radius ( $r$ ) = 3.5 cm

Thickness = 0.7 cm

Outer Radius ( $R$ ) = 3.5 + 0.7  
= 4.2 cm

height ( $h$ ) = 5 dm = 5 × 10 = 50 cm

T.S.A = Inner C.S.A + Outer C.S.A + Area of 2 rings

$$2\pi r h + 2\pi R h + 2(\pi R^2 - \pi r^2)$$

$$= 2\pi (r h + R h + R^2 - r^2)$$

$$= \frac{2 \times 22}{7} (3.5 \times 50 + 4.2 \times 50 + 4.2^2 - 3.5^2)$$

$$= \frac{44}{7} (175 + 210 + 17.64 - 12.25)$$

$$= \frac{44}{7} (385 + 5.39)$$

$$= \frac{44}{7} \times 390.39$$

$$= 44 \times 55.77 = 2453.88 \text{ cm}^2$$

Q7: let breadth of rectangle be  $x$  m  
length be =  $2x$  m

Since sheet is folded to form a cylinder

So Area of sheet = C.S.A. of cylinder

$$l \times b = 1250 \text{ m}^2$$

$$2x \times x = 1250$$

$$x^2 = \frac{1250}{2} = 625$$

$$x = \sqrt{625} = 25 \text{ m}$$

So breadth = 25 m, length = 25 m

Q8: Diameter of roller = 84 cm

$$r = \frac{84}{2} = 42 \text{ cm}$$

length of roller (h) = 120 cm

Area to be leveled = 1584 cm<sup>2</sup>

req. no. of revolutions =  $\frac{\text{Area}}{2\pi rh}$

$$= \frac{1584 \times 100 \times 100 \times 7}{2 \times 22 \times 42 \times 120}$$

$$= 500$$

$$= 500$$

Q9: Total volume of reservoir = 180 m<sup>3</sup>

$$= 108 \times 1000 \quad | \quad 1 \text{ m}^3 = 1000 \text{ l}$$

$$= 108000 \text{ l}$$

Rate of pouring = 60 l/min

$$\text{req. time to fill} = \frac{V}{\text{Rate}} = \frac{108000}{60} \text{ min}$$

$$\frac{1800}{60} = 30 \text{ hrs}$$

Q10: Exterior diameter = 8 cm

$$R = 4 \text{ cm}$$

Thickness = 1 cm

Inner Radius = 3 cm

V. of pipe = Outer V. - Inner V.

$$\begin{aligned}
 & \pi R^2 h - \pi r^2 h \\
 &= \pi h (R^2 - r^2) \\
 &= \frac{22 \times 9100}{7} (4^2 - 3^2) \\
 &= 6600 (16 - 9) \\
 &= 6600 \times 7 \\
 &= 46200 \text{ cm}^3
 \end{aligned}$$

Weight of  $1 \text{ cm}^3$  iron =  $8 \text{ g}$   
 Weight of  $46200 \text{ cm}^3$  iron =  $46200 \times 8$   
 ~~$= 369600 \text{ g}$~~   
 $= 369.6 \text{ kg}$

Q11: Depth of well =  $20 \text{ m}$   
 Diameter =  $7 \text{ m}$   
 Radius =  $\frac{7}{2}$

Length of plot =  $22 \text{ m}$   
 Breadth of plot =  $14 \text{ m}$   
 Let height be  $x \text{ m}$

Since earth taken out from well to get a platform

Volume of platform =  $\pi r^2 h$   
 ~~$22 \times 14 \times h = \frac{22 \times 7 \times 7 \times 20}{7 \times 2 \times 2}$~~

$$h = \frac{5}{2} = 2.5 \text{ m}$$

Q12: Height of cylinder =  $7 \text{ cm}$   
 Volume of cylinder =  $448 \pi$   
 $\pi r^2 h = 448 \pi$

$$r^2 = \frac{448}{h}$$

$$r^2 = \frac{448}{7} = 64$$

$$r^2 = 64, \quad r = 8 \text{ cm}$$

$$\text{L.S.A of cylinder} = 2\pi rh$$

$$2 \times \frac{22}{7} \times 8 \times 7 = 352 \text{ cm}$$

$$\text{T.S.A of cylinder} = 2\pi r(r+h)$$

$$2 \times \frac{22}{7} \times 8(8+7)$$

$$= \frac{2 \times 22 \times 8 \times 15}{7}$$

$$= \frac{5280}{7} = 754.28$$

Q13: For square pyramid =

$$F = 5$$

$$E = 8$$

$$V = 5$$

$$F + V - E = 2$$

$$5 + 5 - 8 = 2$$

$$10 - 8 = 2$$

$$2 = 2$$

$$\text{L.H.S} = \text{RHS}$$

Hence verified

Triangular Prism

$$F = 5$$

$$E = 6$$

$$V = 9$$

$$F + V - E = 2$$

$$5 + 9 - 6 = 2$$

$$2 = 2$$

$$\text{LHS} = \text{RHS}$$

Rectangular pyramid

$$F = 6$$

$$V = 8$$

$$E = 12$$

$$F + V - E = 2$$

$$6 + 8 - 12 = 2$$

$$2 = 2$$

$$\text{LHS} = \text{RHS}$$

Hence verified

HOTS

1.  $\pi r^2 = 154 \text{ unit}^2$

$$r^2 = \frac{154}{\pi}$$

$$r^2 = \frac{154 \times 7}{22}$$

$$r^2 = 49$$

$$r = 7 \text{ cm}$$

C.S.A of cylinder = 880 unit

$$2\pi rh = 880$$

$$2 \times 22 \times 7 \times h = 880$$

$$h = \frac{880}{2 \times 22 \times 7} = 20 \text{ unit}$$

2. Let Breadth of room be  $x$  m

$$\text{length} = x + 50\% \text{ of } x$$

$$= x + \frac{50}{100} \times x$$

$$= x + \frac{x}{2}$$

$$\text{length} = \frac{3x \text{ m}}{2}$$

$$\text{Rate of carpentering} = ₹38.50/\text{m}^2$$

$$\text{Total cost of carpentering} = ₹924$$

$$\text{Area of room} = \frac{924}{38.50}$$

$$\frac{3x \times x}{2} = \frac{924 \times 100}{3850 \times 77}$$

$$x^2 = \frac{24 \times 2}{8}$$

$$x^2 = 16$$

$$x = 4 \text{ m}$$

So breadth is 4 m

$$\text{length} = \frac{3x}{2} = \frac{3 \times 4}{2} = 6 \text{ m}$$

$$\text{Rate of painting 4 walls} = ₹5.50/\text{m}^2$$

$$\text{Total cost of painting 4 walls} = ₹1320$$

$$\text{Area of 4 walls} = \frac{1320}{5.50}$$

$$2h(l+b) = \frac{1320 \times 100}{550}$$

$$2h(6+4) = 240$$

$$2 \times h \times 10 = 240$$

$$h = \frac{240}{10}$$

$$h = 12 \text{ m}$$

~~Done~~  
01/9/22